

$$\tilde{\Sigma} = M^\dagger \sigma_x p M = (1 \otimes \sigma_x - \sigma_y \otimes \sigma_x) \otimes p$$