

$$\langle O \rangle_\psi = \langle \psi | O | \psi \rangle = \langle \Psi | M^\dagger O M | \Psi \rangle =: \langle \tilde{O} \rangle_\Psi$$