

$$V_A(x_B, t) = \frac{-2id_A N v}{\hbar} \frac{d}{dr} \int_0^t dt' \sigma_A^x(t') \int_{-\infty}^{\infty} dk \sin kr e^{-iv k(t-t')}$$