

$$H_0 = \frac{1}{2} \hbar \Omega (\sigma_A^z + \sigma_B^z) + \int_{-\infty}^{\infty} dk \, \hbar \omega_k a_k^\dagger a_k$$