

$$V(x) = i \int_{-\infty}^{\infty} dk \sqrt{N \omega_k} e^{ikx} a_k + \text{H.c.}$$